200 Exam Questions & Answers

Show that (x - 1) is a factor of $x^3 - 3x + 2$. Hence or otherwise factorise $x^3 - 3x + 2$ fully.

22

 $2x^2 + 4x + 7$ is expressed in the form $2(x + p)^2 + q$. What is the value of q.

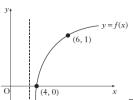
23 If $log_4 12 - log_4 x = log_4 6$, what is the value of x?

Solve $2\cos x = \sqrt{3}$ for x, where $0 \le x < 2\pi$.

- If the exact value of cosx is $\frac{1}{\sqrt{5}}$, find the exact value of cos2x.
- Given that $f(x) = (4 3x^2)^{\frac{-1}{2}}$ on a suitable domain, find f'(x).
- Find the coordinates of the stationary points on the curve $f(x) = x^3 3x + 2$ and determine their nature.
- **28** Find $\int \left(4x^{\frac{1}{2}} + x^{-3}\right) dx$, where x > 0.
- The graph of y = f(x) passes through the point $\left(\frac{\pi}{9}, 1\right)$. If $f'(x) = \sin(3x)$ express y in terms of x.
- Write sinx cosx in the form ksin(x a) stating the values of k and a where k > 0 and $0 \le a \le 2\pi$.

31	Functions f and g are given by $f(x) = 3x + 1$
	and $g(x) = x^2 - 2$.
	Find $f(g(x))$ and $g(f(x))$.

32 The diagram shows the graph of y = f(x) where f is a logarithmic function. What are the values of a and b for $(x) = log_a(x - b)$?



- The vectors $\mathbf{u} = \begin{pmatrix} k \\ -1 \\ 1 \end{pmatrix}$ and $\mathbf{v} = \begin{pmatrix} 0 \\ 4 \\ k \end{pmatrix}$ are perpendicular. What is the value of k?
- **34** D, E and F have coordinates (10, -8, -15), (1, -2, -3) and (-2, 0, 1) respectively. Show that D, E and F are collinear and find the ratio in which E divides DF.
- Prove that $\frac{\cos^3 x}{1-\sin^2 x} = \cos x$.
- The line L passes through the point (-2, -1) and is parallel to the line with equation 5x + 3y 6 = 0. What is the equation of L?
- Triangle PQR has vertices at P(-3,-2), Q(-1,4) and R(3,6). PS is a median. What is the gradient of PS?
- The diagram shows a circle, centre (2, 5) and a tangent drawn at the point (7, 9). What is the equation of this tangent?



- A sequence is generated by the recurrence relation $u_{n+1} = 0.4u_n 240$. What is the limit of this sequence as $\rightarrow \infty$?
- 40 Calculate the shaded area enclosed by the curve $y = x^3(3 x)$ and the x-axis between x = 0 and x = 3.

