200 Exam Questions & Answers

161 Show that (x + 2) is a factor of $f(x) = x^3 - 2x^2 - 4x + 8$ and hence fully factorise f(x).

162

Calculate the discriminant of the quadratic equation $2x^2 + 4x + 5 = 0$

163

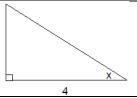
Solve the equation $log_4(5-x) - log_4(3-x) = 2$, x < 3.

164

Find all the values of x in the interval $0 \le x \le 2\pi$ for which $tan^2(x) = 3$.

165

Show that the exact value of cos2x is $\frac{7}{25}$.



166

If
$$y = 3\cos^4 x$$
, find $\frac{dy}{dx}$.

167
A curve has equation $y = x^3 - 3x^2 - 9x + 12$. Find the coordinates of the stationary points of this curve and determine their nature.

168

Find
$$\int \frac{4x^3-1}{x^2} dx$$
, $x \neq 0$.

169

Find the value of $\int_0^2 \sin(4x+1) dx$.

170

A curve has equation y = 7sinx - 24cosx. Express 7sinx - 24cosx in the form ksin(x - a)where k > 0 and $0 \le a \le \frac{\pi}{2}$.

$$f(x) = 3x - 1 \text{ and } g(x) = \frac{1}{x+1}$$

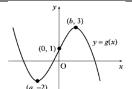
Find $f(g(x))$ and $g(f(x))$.

State a suitable domain for g(f(x)).

172 The diagram shows the

graph
$$y = g(x)$$
.

- a. Sketch y = -g(x)
- b. Sketch y = 3 g(x)



173

If
$$f = 3i + 2k$$
 and $g = 2i + 4j + 3k$, Find $|f + g|$.

174

Express the vectors \overrightarrow{TA} and \overrightarrow{TB} in component form.

Calculate the angle between \overrightarrow{TA} and \overrightarrow{TB} .

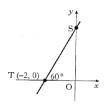
175

Prove the identity:

$$(\cos P^{\circ} + \sin P^{\circ})^{2} = 2\sin P^{\circ} \cos P^{\circ} + 1$$

176

Find the equation of the line ST, where T is the point (-2, 0) and angle STO is 60° .



177

Triangle ABC has vertices A(-1, 12), B(-2, -5) and C(7, -2). Find the equation of the altitude AE.

178

Show that the line with equation y = 6 - 2x in a tangent to the circle with equation $x^2 + y^2 + 6x - 4y - 7 = 0$ and find the coordinates of the point of contact of the tangent and the circle.

179 A sequence is defined by the recurrence relation $u_{n+1} = 0.2u_n + 5$ with $u_8 = 20$. Calculate u_{10} .

180

Calculate the area enclosed between the curve $y = x^2 - 6x$ and the x-axis.

