200 Exam Questions & Answers

141

Show that (x - 4) is a factor of $x^3 - 5x^2 + 2x + 8$. Hence, fully factorise and solve $x^3 - 5x^2 + 2x + 8$.

142

Solve $6 - x - x^2 < 0$

143

Before a forest fire was brought under control, the spread of the fire was described by a law of the form $A=A_0e^{kt}$ where A_0 is the area covered by the fire when it was first detected and A is the area covered by the fire t hours later. If it takes 1.5 hours for the area of the forest fire to double, find the value of the constant k.

144

Solve $2 \sin(2x - 60)^{\circ} = 1$ for $0 \le x \le 360$.

145

Using $75^\circ=45^\circ+30^\circ$, ${\rm show\ that\ } sin 75^\circ=\frac{\sqrt{6}+\sqrt{2}}{4}.$

146

If $y = 3x^{-2} + 2x^{\frac{3}{2}}$, x > 0, determine $\frac{dy}{dx}$

147

The parabola with equation $y = x^2 - 14x + 53$ has a tangent at the point P(8, 5). Find the equation of this tangent.

148

Find $\int \frac{(x^2-2)(x^2+2)}{x^2} dx$, $x \neq 0$

149

The curve y = f(x) is such that $\frac{dy}{dx} = 4x - 6x^2$.

The curve passes through the point (-1, 9).

Express y in terms of x.

150

Express $3cosx^{\circ} + 4sinx^{\circ}$ in the form $kcos(x - a)^{\circ}$ Hence, solve $3cosx^{\circ} + 4sinx^{\circ} = 5$



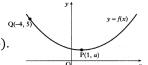
$$f(x) = 8x^2 - 5$$
 and $g(x) = 5 + x$

Find f(g(x)) and g(f(x)).

152 The diagram shows the graph of a

function y = f(x). Sketch the graphs of:

y = f(x - 4) and y = 2 + f(x - 4).



153

A(0, -3, 5), B(7, -6, 9) and C(21, -12, 17).

Show that A, B and C are collinear, stating the ratio AB:BC.

154 P is the point (-1, 2, -1) and Q is (3, 2, -4). Write down PQ in component form. Calculate the length of \overrightarrow{PQ} .

Find the components of a unit vector which is parallel to \overrightarrow{PQ} .

155

Prove the identity:

$$\cos^2 Q \tan^2 Q = 1 - \cos^2 Q$$

156

The point A has coordinates (7, 4). The straight lines with equations x + 3y + 1 = 0 and

2x + 5y = 0 intersect at B.

Find the gradient of AB.

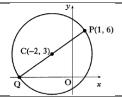
157

A triangle has vertices A(5, 5), B(-10, 0) and

C(0, -10). Find the equation of the altitude from A.

158

A circle has centre C(-2, 3) and passes through P(1, 6). Find the equation of the circle.



159 A sequence is defined by the recurrence relation

 $u_{n+1} = 0.8u_n + 12$, $u_0 = 4$.

State why this sequence has a limit and find this limit.

160

Calculate the area between the line y = x + y = 18 and the curve $y = x^2 - 8x + 18$.

