

Surds

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Graduate Bsc (Hons) MathsSci (Open) GIMA

A surd can simply be defined as the root of a number which does not have an exact decimal equivalent.

e.g. $\sqrt{3} = 1.732\dots$ Is a surd

$\sqrt{25} = 5$ Is not a surd

It is common place in the exams to be asked to simplify a given surd. To simplify a surd we use the basic rules of arithmetic, especially multiplication and division.

It is essential that you know the following:-

$$s = \sqrt{s} \cdot \sqrt{s}$$

$$33 = \sqrt{33} \cdot \sqrt{33}$$

$$\sqrt{s} \cdot \sqrt{s} = s$$

$$\sqrt{33} \cdot \sqrt{33} = 33$$

$$\sqrt{s} + \sqrt{s} = \sqrt{s}(1 + 1) = 2\sqrt{s}$$

$$\sqrt{33} + \sqrt{33} = \sqrt{33}(1 + 1) = 2\sqrt{33}$$

$$\sqrt{mn} = \sqrt{m} \cdot \sqrt{n}$$

$$\sqrt{3 \cdot 2} = \sqrt{3} \cdot \sqrt{2} = \sqrt{6}$$

$$\sqrt{m} \cdot \sqrt{n} = \sqrt{mn}$$

$$\sqrt{3} \cdot \sqrt{2} = \sqrt{6}$$

$$(a + \sqrt{b})(a - \sqrt{b}) = a^2 + a\sqrt{b} - a\sqrt{b} - b = a^2 - b$$

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Some examples

Simplify the following

$$\sqrt{12} = \sqrt{4 \cdot 3} = 2\sqrt{3}$$

$$\sqrt{96} = \sqrt{32 \cdot 3} = \sqrt{16 \cdot 2 \cdot 3} = 4\sqrt{2 \cdot 3} = 4\sqrt{6}$$

$$\sqrt{48} = \sqrt{16 \cdot 3} = 4\sqrt{3}$$

$$\sqrt{18} = \sqrt{9 \cdot 2} = 3\sqrt{2}$$

More complicated questions ask you to rationalise the denominator of an expression whose denominator is a surd. Rationalise simply means to not have any root signs in the denominator. These type of questions are all done by the same method.

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Example of rationalising

Rationalise the following expression

$$\frac{1}{(c + \sqrt{d})}$$

Method: Using the rules of arithmetic multiply top and bottom by

$$c - \sqrt{d}$$

This will make the denominator the difference of two squares and will eliminate any root signs in the denominator. We have:-

$$\frac{1}{(c + \sqrt{d})} = \frac{1}{(c + \sqrt{d})} \cdot \frac{(c - \sqrt{d})}{(c - \sqrt{d})} = \frac{(c - \sqrt{d})}{[c^2 - c\sqrt{d} + c\sqrt{d} - (\sqrt{d})^2]} = \frac{(c - \sqrt{d})}{(c^2 - d)}$$

Rationalise the following expression

$$\frac{2}{(1 - \sqrt{3})}$$

Method: Using the rules of arithmetic multiply top and bottom by

$$(1 + \sqrt{3})$$

Not this time since the denominator has a minus sign in the middle we multiply by a plus sign in the middle. You always multiply by the opposite sign so you are guaranteed to have no roots in the denominator. We have:-

$$\frac{2}{(1 - \sqrt{3})} = \frac{2}{(1 - \sqrt{3})} \cdot \frac{(1 + \sqrt{3})}{(1 + \sqrt{3})} = \frac{2 \cdot (1 + \sqrt{3})}{[1^2 - \sqrt{3} + \sqrt{3} - (\sqrt{3})^2]} = \frac{2 \cdot (1 + \sqrt{3})}{(-2)} = -(1 + \sqrt{3})$$